

# OpenParEM3D

Electromagnetic Simulator

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# Agenda

- Motivation
- Features
- S-parameters
- 3D FEM setup
- Adaptive mesh refinement
- Examples and discussion
- Regression suites
- Conclusion

# Motivation

- Lack of a free or very low-cost frequency-domain S-parameter electromagnetic simulator inhibits exploration of new ideas and development of new products
- Target audience
  - Engineers wanting to explore ideas at home
  - Continuing education
  - Students
  - Small startups
- Feasibility
  - Leverage existing open-source projects
  - CAD (FreeCAD), meshing (gmsh), FEM (MFEM), visualization (ParaView)
  - “Just” need to glue it all together

# Features

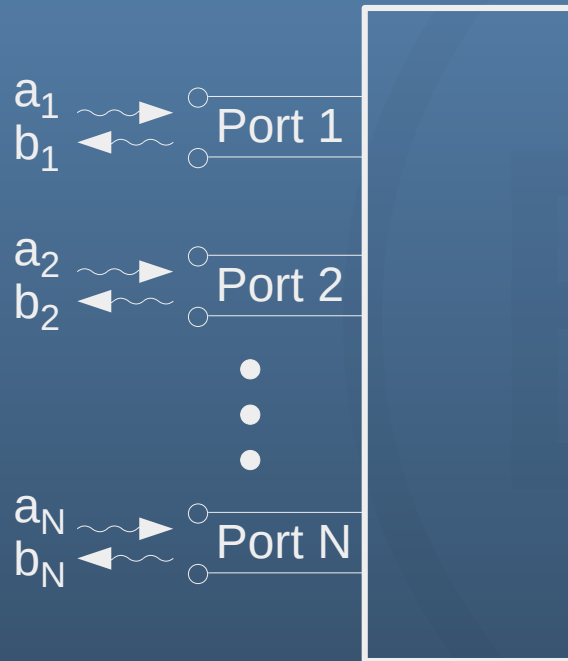
- Full-wave time-harmonic 3D electromagnetic simulator
- Computing
  - Electric and magnetic fields
  - S-parameters between 2D ports on the surface of the 3D space
- Arbitrary high-order elements
  - courtesy of MFEM, ParaView [up to 6<sup>th</sup> order]
- Parallel processing via MPI
  - courtesy of MFEM, PETSc, and SLEPc plus custom code
- Adaptive mesh refinement
  - courtesy of MFEM plus custom code
- TBD: impedance boundary condition for conductor losses and antennas

# S-parameters

- “S-parameters” is short for “scattering parameters”
  - Links incident and reflected waves at the ports of a 3D volume
- Dominant in engineering to include electromagnetic results in circuit simulations and for performance analyses
- A “must have” output for a practical simulator

# S-parameter Matrix Extraction

Propagating waves are modes on transmission lines or waveguides feeding N ports.



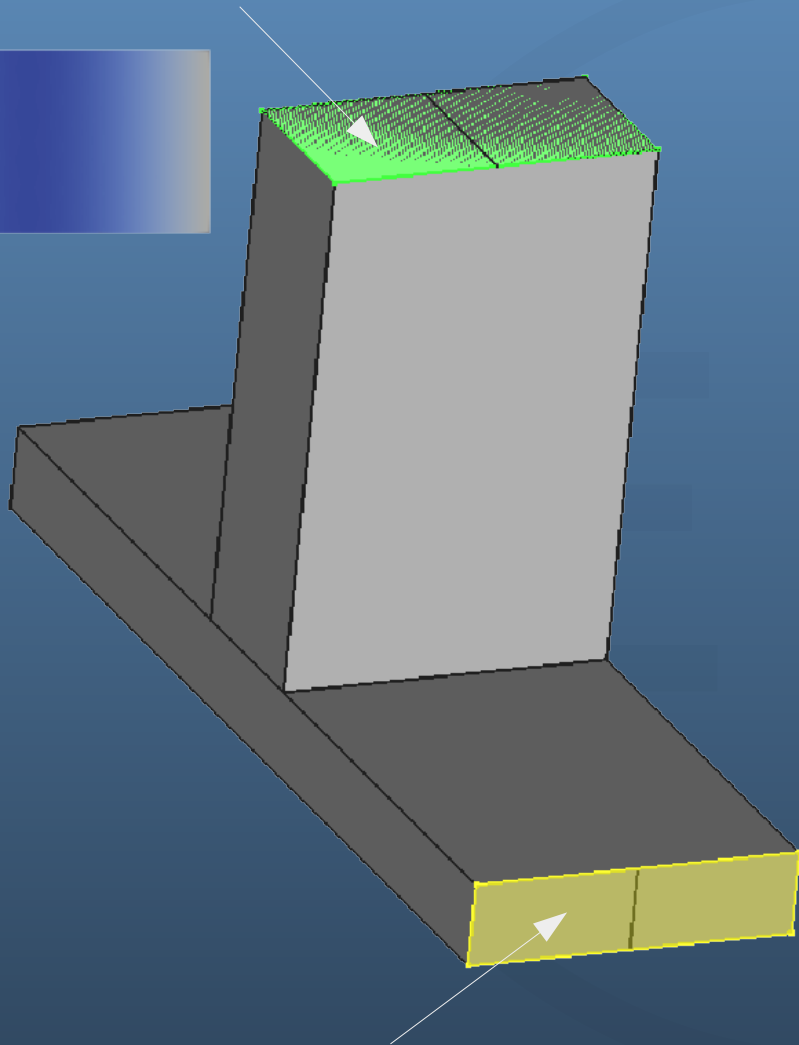
$a_i$  is the incident wave to port i  
 $b_i$  is the reflected wave from port i

$$\begin{matrix} \text{S-parameter matrix} \\ \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_N \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} & \cdots & S_{1N} \\ S_{21} & S_{22} & \cdots & S_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ S_{N1} & S_{N2} & \cdots & S_{NN} \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_N \end{bmatrix} \end{matrix}$$

- Define ports - 2D (flat) on surface of 3D space
- Solve 1 column at a time
  - Drive port i such that  $a_i \neq 0$
  - Apply absorbing boundary condition on all other ports, then  $a_k = 0$  for  $k \neq i$
- Solve the 3D problem N times for  $i=1,\dots,N$
- Separate  $a_i$  and  $b_i$  at the driven port
- Output frequency-dependent S-parameters in Touchstone file format

# Driving $a_i$

Port i: 2D simulation for fields,  $\alpha$ ,  $\beta$ ,  $Z_0$



Port k: absorbing boundary

- MFEM's ParSubMesh functionality is used to extract 2D meshes
- A 2D simulation is run for each port with OpenParEM2D\*
- The 2D field solution for port i is applied to the 3D space, forcing the 3D fields at the port to take the 2D configuration
- An absorbing boundary condition is applied at the other ports
- 3D electromagnetic simulation is run
- Repeat for each port
- Extract S-parameters (more later)

\* OpenParEM2D was presented at the 2022 MFEM Community Workshop.

# 3D FEM Setup

- Weak form of the wave equation in  $\bar{E}$

$$\iiint_{\Omega} \frac{1}{\bar{\mu}_r} \nabla \times \bar{E} \cdot \nabla \times \bar{W} dV - k_0^2 \iiint_{\Omega} \epsilon_r \bar{E} \cdot \bar{W} dV + \iint_S \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS = 0$$

MFEM  
CurlCurlIntegrator

MFEM  
VectorFEMassIntegrator

Surface of the 3D space

- Separate the surface integral

$$\iint_S \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS = \iint_{S_b} \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS + \sum_{i=1}^N \iint_{S_{pi}} \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS$$

PEC and/or PMC boundary  
Apply BC directly to the matrix  
[DOF=0 for PEC, keep DOF for PMC]

N ports



# 2D Port Setup on Surface

- Setup of the surface integral (from prior slide)

$$\iint_S \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS = \iint_{S_b} \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS + \sum_{i=1}^N \iint_{S_{pi}} \frac{1}{\bar{\mu}_r} \hat{n} \times \nabla \times \bar{E} \cdot \bar{W} dS$$

DOF manipulation Not Supported in MFEM

- Apply a propagating assumption at the ports
  - A first-order absorbing boundary condition

$$\begin{aligned} \hat{n} \times \nabla \times \bar{E} &= -\frac{\partial \bar{E}_t}{\partial n} + \nabla_t E_n && \leftarrow \text{Identity} \\ &= \gamma \bar{E}_t + \nabla_t E_n && \leftarrow \text{Propagation Assumption} \quad \frac{\partial \bar{E}_t}{\partial n} = \frac{\partial \bar{E}(t) e_t^{-\gamma n}}{\partial n} = -\gamma \bar{E}(t) \end{aligned}$$

MFEM  
VectorFEMassIntegrator

Not supported in MFEM for Nedelec elements

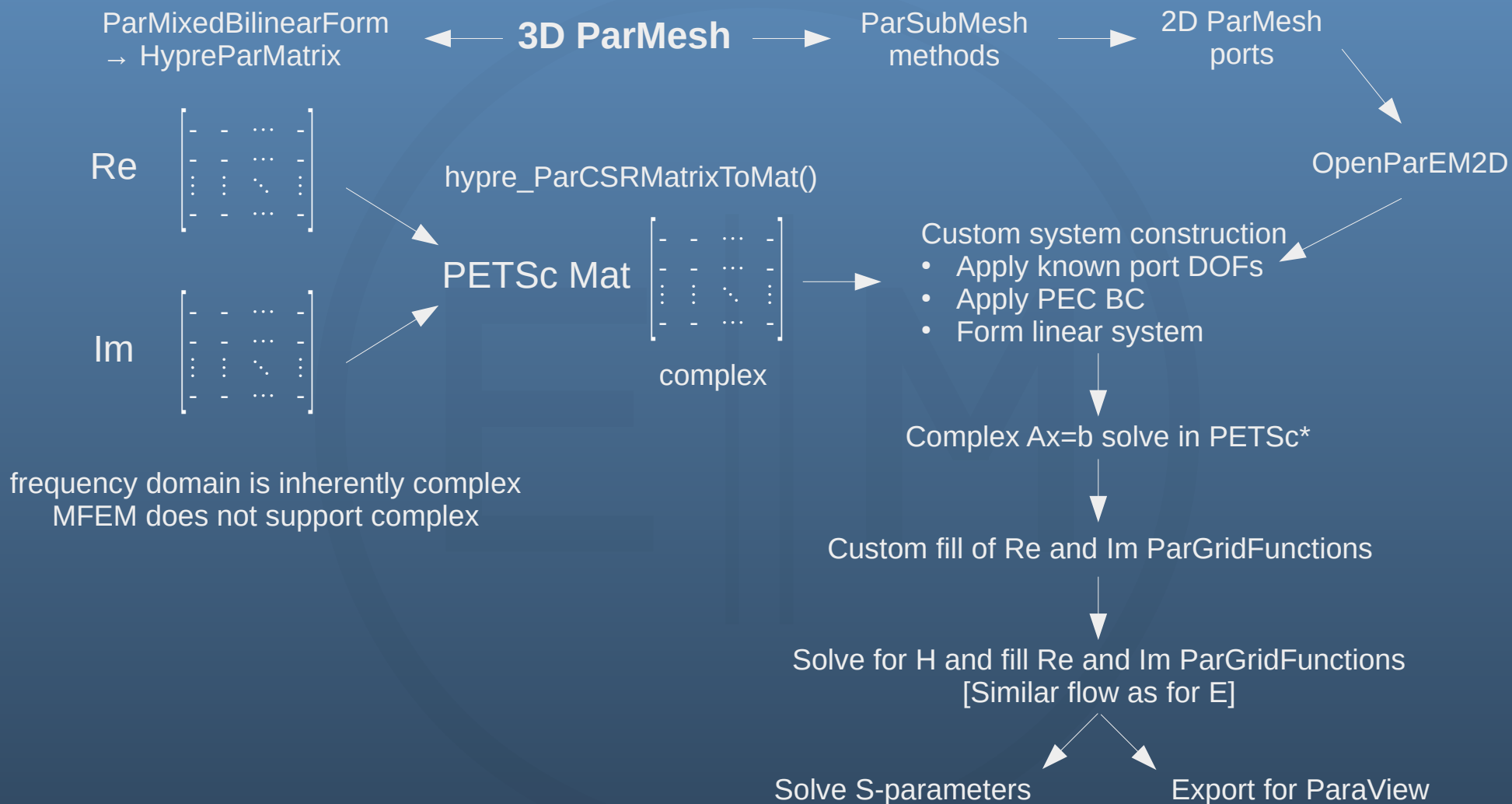
- Normal component on the boundary
- Assume that this term is negligible

# On the Neglected Gradient Term

- On the port boundaries, the gradient term of the normal component is neglected
- A zero gradient of a non-zero  $E_n$  is not physically realizable
  - This means that it is assumed that  $E_n=0$
- The implemented boundary condition strictly only applies to transverse electric modes (TE and TEM)
  - TE and TEM cases dominate problems of interest. These include microstrip, stripline, coax, triax, slot line, coplanar waveguide, the TE10 mode in rectangular waveguide, and generally, any N-conductor transmission line
  - So the TE restriction in practice is not significantly limiting
- Non-TE modes suffer field distortion at the port leading to a reflection
- Non-TE modes at the boundaries can be supported by using TE modes at the ports with 3D transitions to the required non-TE ports followed by de-embedding (like lab measurements)
- For quasi- TE and TEM modes,  $E_n$  is small compared to  $\bar{E}_t$ 
  - The error caused by the reflection is determined by the strength of  $E_n$
  - For quasi- TE and TEM modes, the reduction in accuracy may be acceptable
- Future work is needed to relax this restriction, for example, by including the gradient term or by implementing a perfectly matched layer (PML) boundary condition

# Top-Level Implementation Details

Start Here



\* A real formulation was tried in MFEM, but poor convergence was observed. For background, see David Day and Mike Heroux, "Solving Complex-valued Linear Systems via Equivalent Real Formulations", report from Sandia National Laboratories, May 9, 2000. There is a later SIAM paper based on this work.

# $S_{ii}$ : Separating $a_i$ and $b_i$

- At this point, the 3D fields for  $\bar{E}$  and  $\bar{H}$  are computed.
  - The E-field from the 2D port simulation was applied at port  $i$  [i.e. the driving port]
  - Cannot differentiate  $\bar{E}^+$  from  $\bar{E}^-$  just from the port  $i$  E-field.
  - Requires  $\bar{H}$  to separate the two
- Just use the tangential components since they dominate in practical applications

# At Port i, the Driving Port

$$\overline{E}_{ti} = C_{1i} \overline{E}_{ti}^+ + C_{2i} \overline{E}_{ti}^- \quad \leftarrow \text{Split with weights}$$

$$\iint_{S_i} \overline{E}_{ti}^{+*} \cdot \overline{E}_{ti} dS = C_{1i} \iint_{S_i} \overline{E}_{ti}^{+*} \cdot \overline{E}_{ti}^+ dS + C_{2i} \iint_{S_i} \overline{E}_{ti}^{+*} \cdot \overline{E}_{ti}^- dS \quad \leftarrow \text{Inner products supported by MFEM}$$

$$\overline{E}_{ti}^- = \overline{E}_{ti}^+$$

$$\iint_{S_i} \overline{E}_{ti}^{+*} \cdot \overline{E}_{ti} dS = C_{1i} \iint_{S_i} \overline{E}_{ti}^{+*} \cdot \overline{E}_{ti}^+ dS + C_{2i} \iint_{S_i} \overline{E}_{ti}^{+*} \cdot \overline{E}_{ti}^+ dS \quad \rightarrow e_{0i} = (C_{1i} + C_{2i}) e_{2i}$$

$$\overline{H}_{ti} = C_{1i} \overline{H}_{ti}^+ + C_{2i} \overline{H}_{ti}^- \quad \leftarrow \text{Same mode, same weights}$$

$$\iint_{S_i} \overline{H}_{ti}^{+*} \cdot \overline{H}_{ti} dS = C_{1i} \iint_{S_i} \overline{H}_{ti}^{+*} \cdot \overline{H}_{ti}^+ dS + C_{2i} \iint_{S_i} \overline{H}_{ti}^{+*} \cdot \overline{H}_{ti}^- dS$$

$$\overline{H}_{ti}^- = -\overline{H}_{ti}^+ \quad \leftarrow \text{Note the change in sign}$$

$$\iint_{S_i} \overline{H}_{ti}^{+*} \cdot \overline{H}_{ti} dS = C_{1i} \iint_{S_i} \overline{H}_{ti}^{+*} \cdot \overline{H}_{ti}^+ dS - C_{2i} \iint_{S_i} \overline{H}_{ti}^{+*} \cdot \overline{H}_{ti}^+ dS \quad \rightarrow h_{0i} = (C_{1i} - C_{2i}) h_{2i}$$

$$C_{1i} = \frac{1}{2} \begin{pmatrix} e_{0i} + h_{0i} \\ e_{2i} + h_{2i} \end{pmatrix}$$

$$C_{2i} = \frac{1}{2} \begin{pmatrix} e_{0i} - h_{0i} \\ e_{2i} + h_{2i} \end{pmatrix}$$

# S<sub>ii</sub>

- $\bar{E}^+$  is the +z direction in OpenParEM2D
  - Away from the 3D space, so related to b
  - $\bar{E}^-$  is then related to a

- Voltage wave relationships to S:  $a_i = \frac{V_i^+}{\sqrt{Z_{oi}}}$      $b_i = \frac{V_i^-}{\sqrt{Z_{oi}}}$

- Proportional to the weights:  
(field structure is the same)  $a_i = \frac{C_{2i}}{\sqrt{Z_{oi}}}$      $b_i = \frac{C_{1i}}{\sqrt{Z_{oi}}}$

- S<sub>ii</sub>:

$$S_{ii} = \frac{b_i}{a_i} = \left( \frac{e_{0i}}{e_{2i}} + \frac{h_{0i}}{h_{2i}} \right) / \left( \frac{e_{0i}}{e_{2i}} - \frac{h_{0i}}{h_{2i}} \right)$$

# S<sub>ji</sub>

- Use direct calculation with voltages\*

Integrate at the output port (no reverse wave):  $V_j^+ = V_j$

Integrate at the input port, then take the fraction traveling towards the 3D space:  $V_i^- = C_{2i} V_i$

Use power/voltage definition for  $Z_o$

$$S_{ji} = \frac{b_j}{a_i} = \left( \frac{V_j^+}{\sqrt{Z_{oj}}} \right) / \left( \frac{V_i^-}{\sqrt{Z_{oi}}} \right)$$

- S<sub>ji</sub>:

$$S_{ji} = \frac{b_j}{a_i} = \left( \frac{V_j}{\sqrt{Z_{oj}}} \right) / \left( \frac{C_{2i} V_i}{\sqrt{Z_{oi}}} \right)$$

\* Can also use currents, which is a future upgrade, to enable the power/current definition of  $Z_o$ .

# Adaptive Mesh Refinement (AMR)

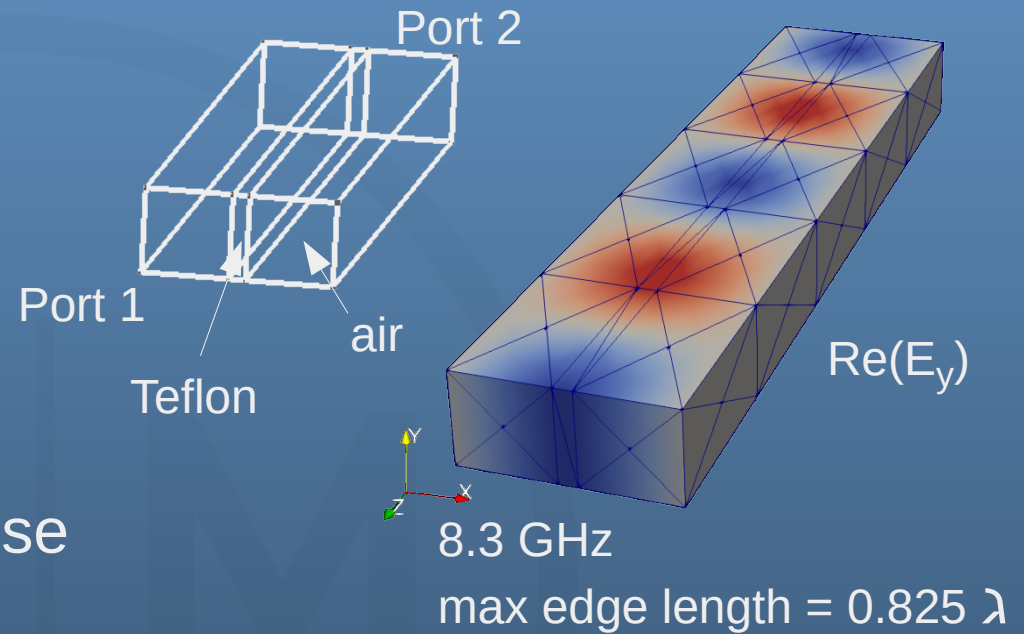
- Follows the setup used in the MFEM Tesla miniapp
  - CurlCurlIntegrator on  $\bar{E}$ , RT elements for flux, and ND elements for smoothed flux
  - Merge errors from both  $\text{Re}(\bar{E})$  and  $\text{Im}(\bar{E})$
- Extract errors from several solutions
  - Per driven port
  - Combine across all driven ports
  - Apply threshold refinement with a cap on the number of elements to refine
- Refine using `ParMesh::GeneralRefinement`
- Convergence test is on  $S$ . Calculate an error criteria at the  $N$ th iteration
  - $\text{error} = \max \text{ column norm } \{ \bar{S}_N^{-1} (\bar{S}_N - \bar{S}_{N-1}) \}$
- Options for sequential number of iterations that must meet the convergence criteria
- Options for AMR at multiple frequencies
- Issue? Degradation of mesh quality with each iteration, especially at ports



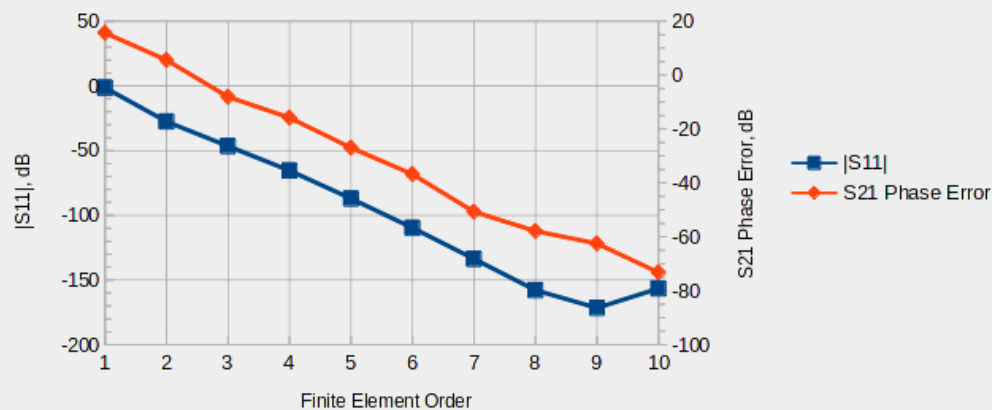
# Examples and Discussion

# WR90 Loaded Rectangular Waveguide

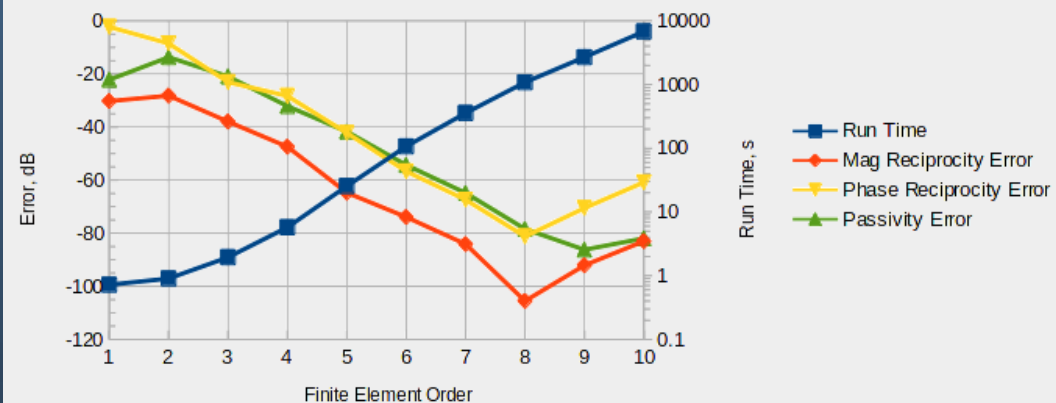
- Exact solution
  - $|S_{11}|$  in dB  $\rightarrow -\infty$
  - phase shift from high-resolution OpenParEM2D simulation
- High accuracy with regular improvement to a very low noise floor



P Convergence at 8.3 GHz

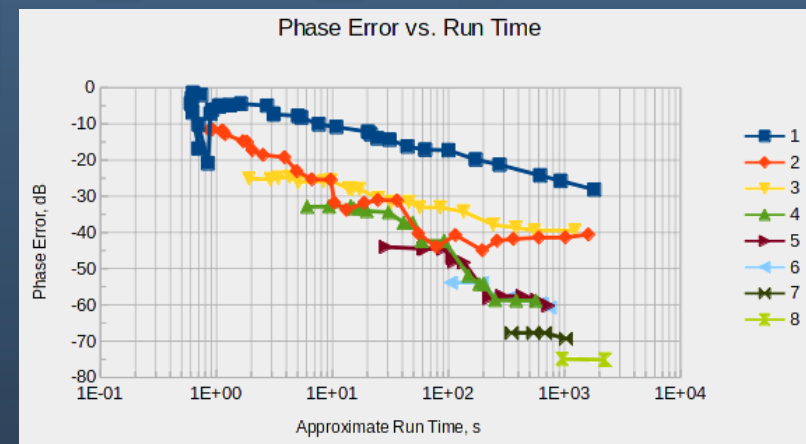
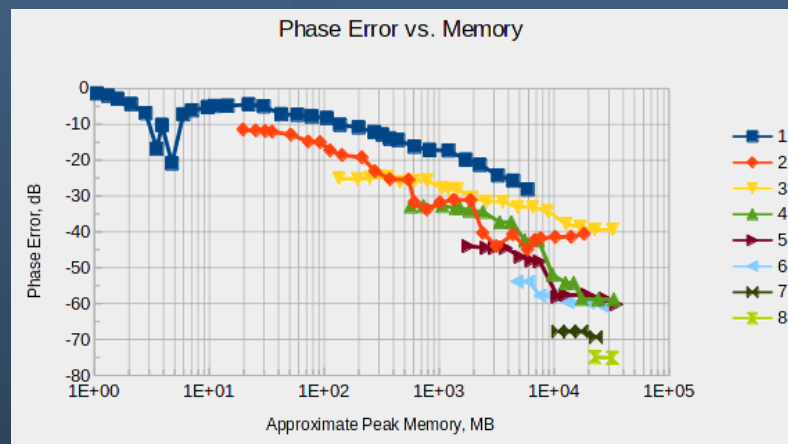
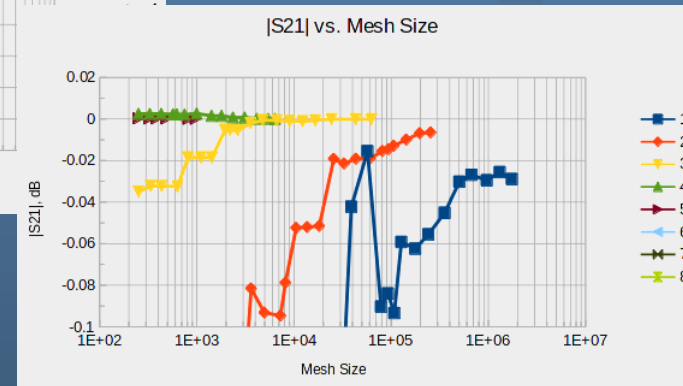
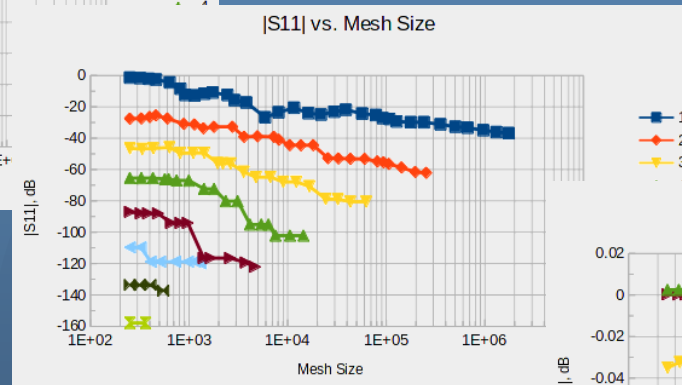
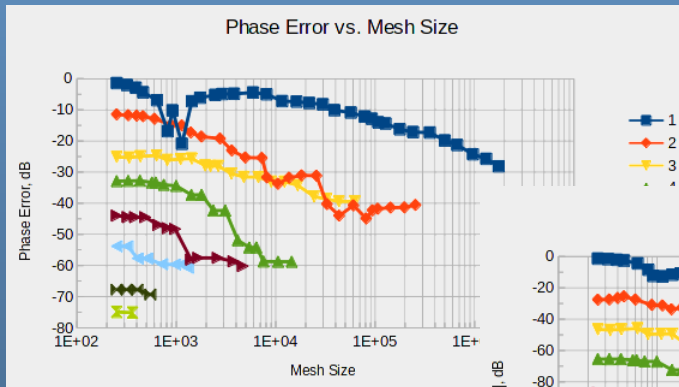


Self Consistency and Run Time



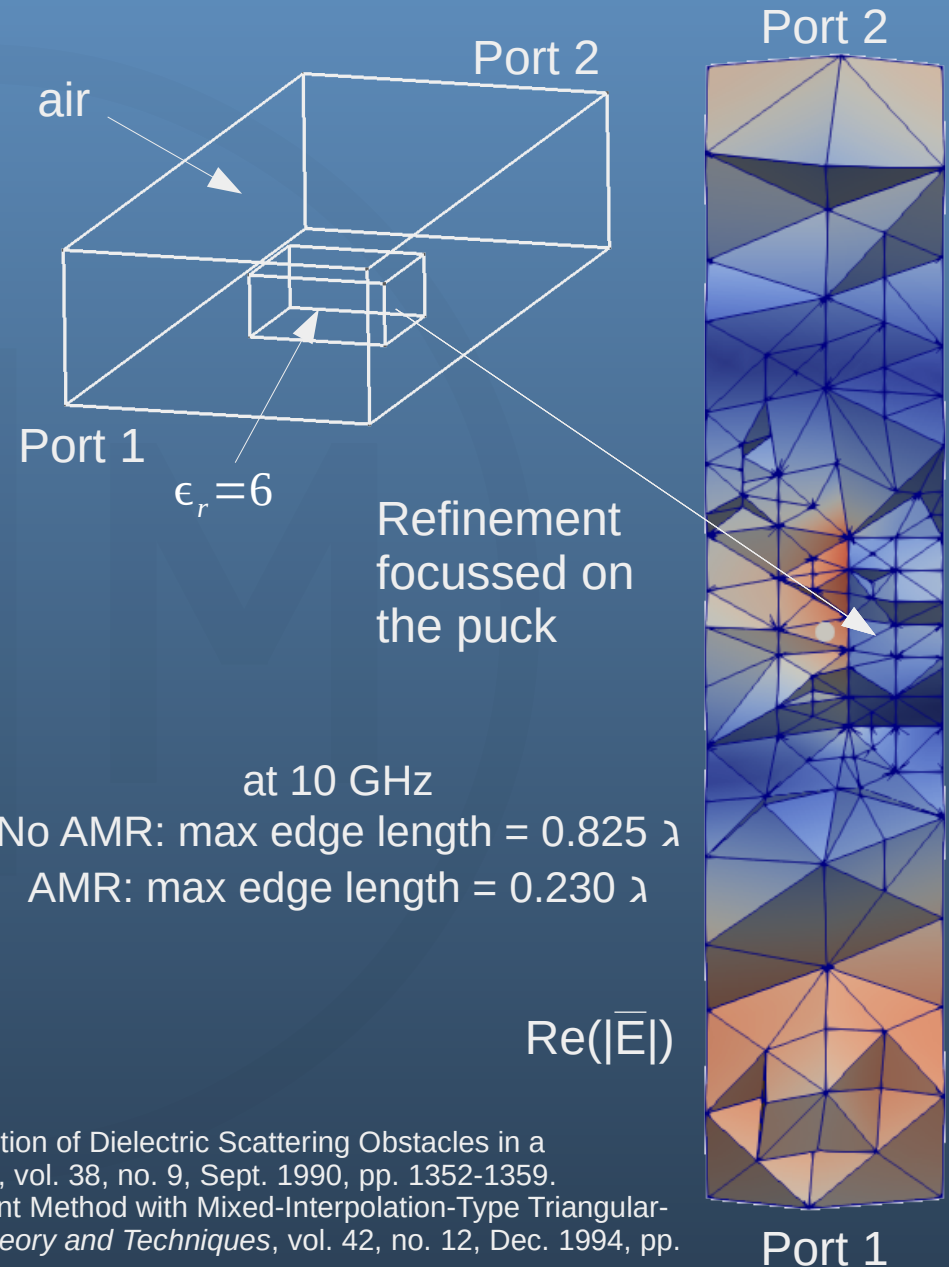
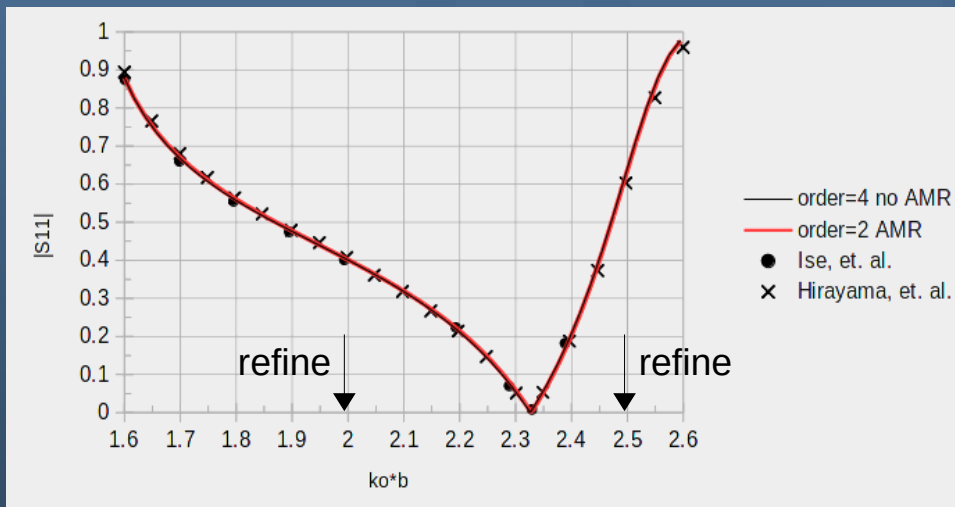
# h-Convergence with AMR

- WR90 loaded rectangular waveguide at 8.3 GHz
- Effective AMR
- Accuracy improves with AMR and FEM order
- Favor FEM order over iterations



# WR75 with Dielectric Puck

- Solve with and without AMR
  - 2<sup>nd</sup> order, AMR: 575 s
  - 4<sup>th</sup> order: 968 s
- Excellent agreement between runs with and without AMR
- Excellent agreement between this and prior work

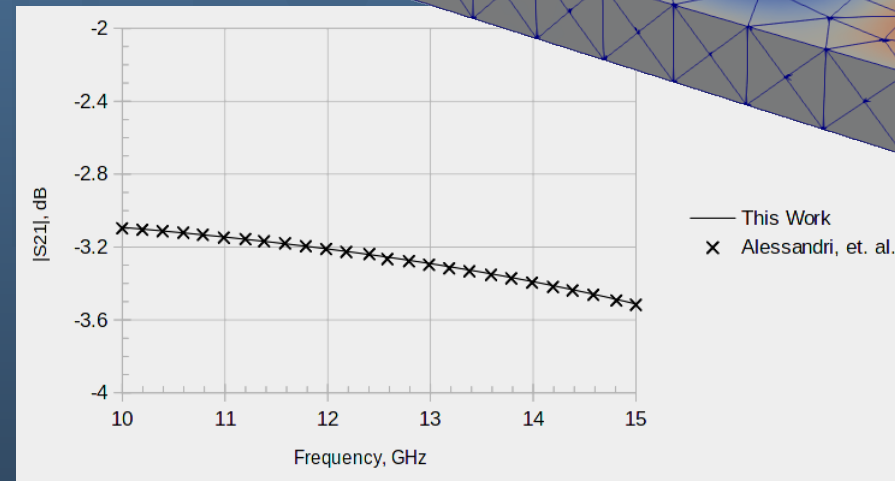
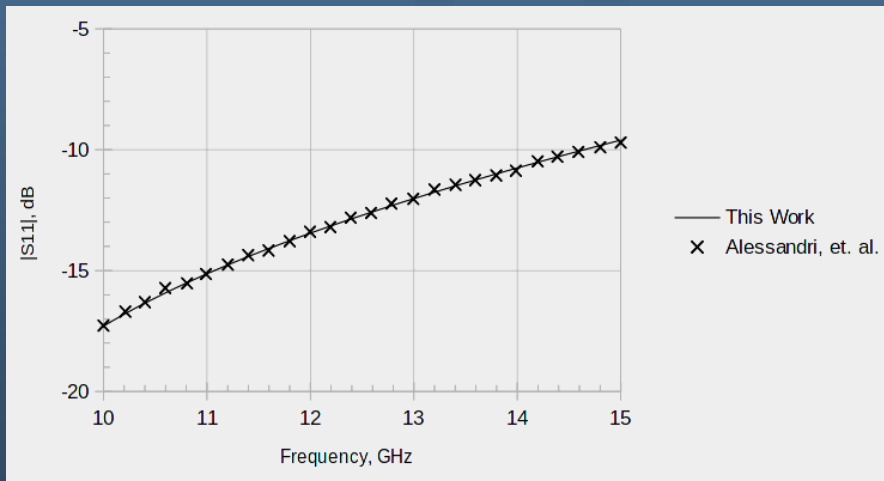
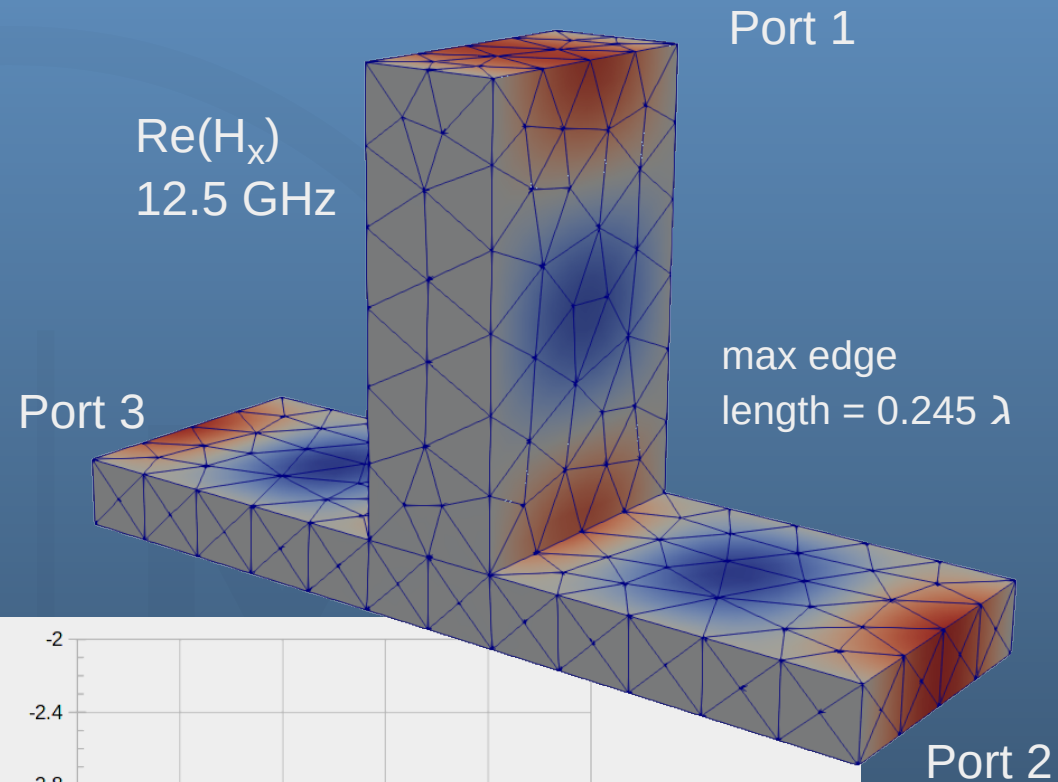


at 10 GHz  
 No AMR: max edge length =  $0.825 \lambda$   
 AMR: max edge length =  $0.230 \lambda$

- K. Ise, K. Inoue, and M. Koshiba, "Three-Dimensional Finite-Element Solution of Dielectric Scattering Obstacles in a Rectangular Waveguide," *IEEE Trans. Microwave Theory and Techniques*, vol. 38, no. 9, Sept. 1990, pp. 1352-1359.
- K. Hirayama, Md. Alam, Y. Hayashi, and M. Koshiba, "Vector Finite Element Method with Mixed-Interpolation-Type Triangular-Prism Element for Waveguide Discontinuities", *IEEE Trans. Microwave Theory and Techniques*, vol. 42, no. 12, Dec. 1994, pp. 2311-2316.

# WR75 Waveguide T-Junction

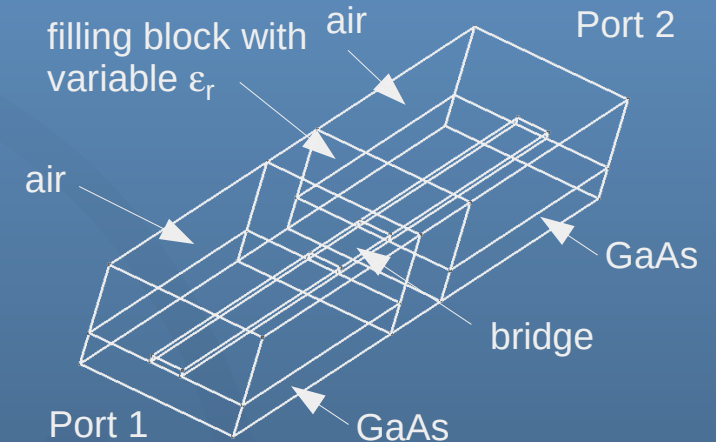
- WR75 lossless waveguide splitting to two half-height waveguides for an even power split
- 4<sup>th</sup> order elements with no adaptive refinement
- Excellent agreement between this work and the referenced paper



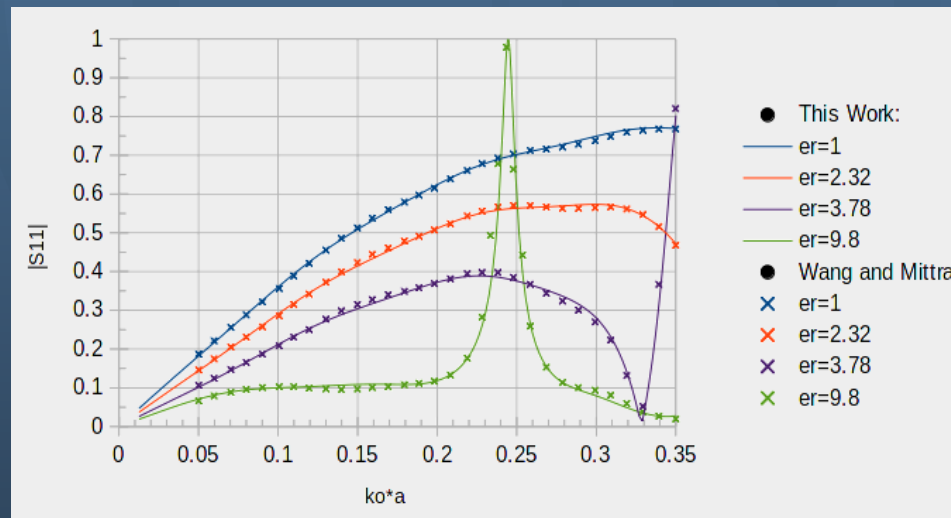
- F. Alessandri, M. Dionigi, and R. Rorrentino, “Rigorous Analysis of Compensated E-plane Junctions in Rectangular Waveguide,” *1995 IEEE MTT-S Digest*, pp. 987-990.

# Microstrip Bridge

- Microstrip on GaAs bridging across a gap through a block of variable dielectric constant material
- 5<sup>th</sup> order elements with no adaptive refinement
  - Use the same mesh throughout



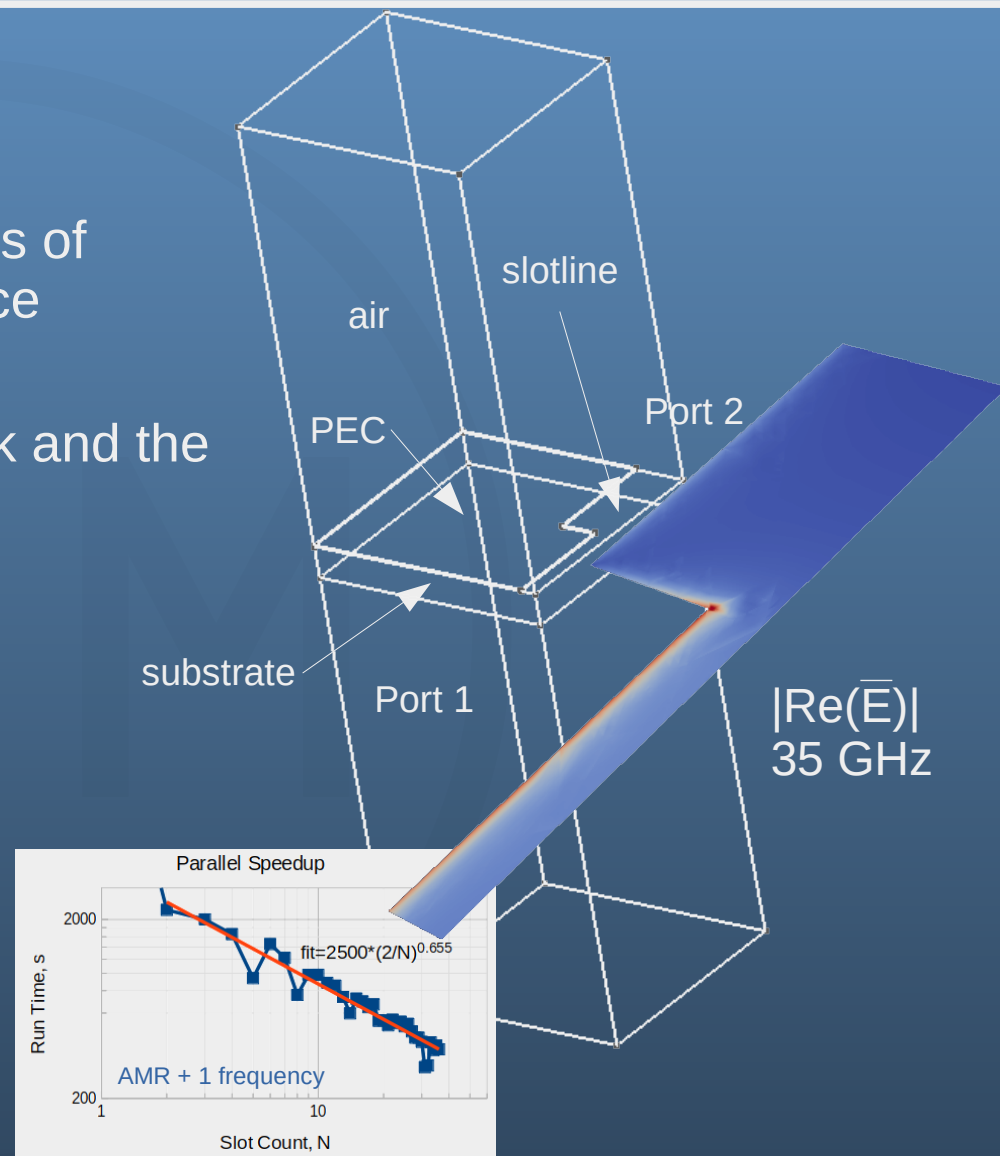
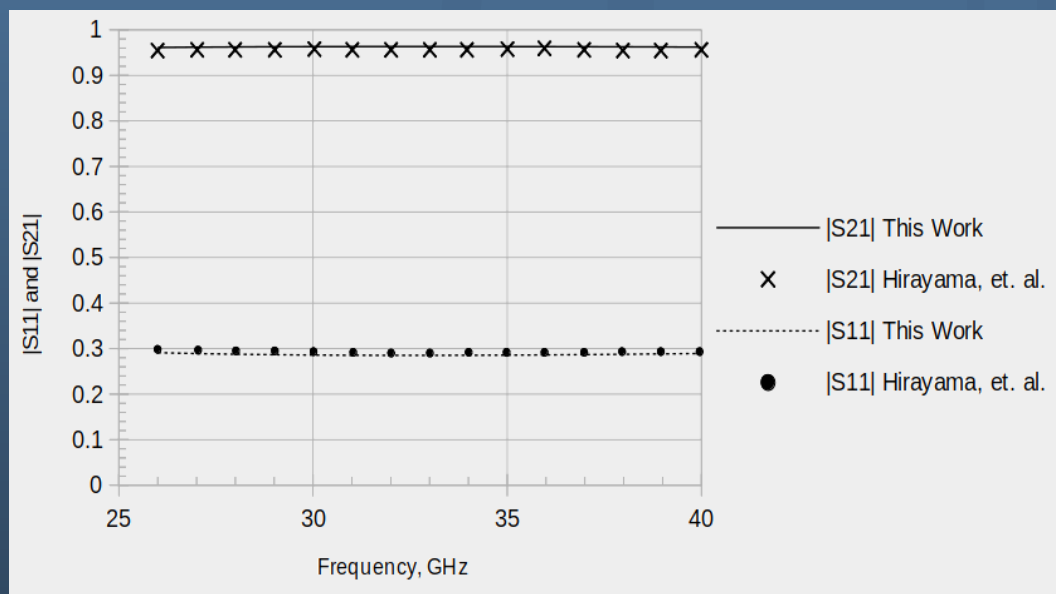
- Excellent agreement between this work and the referenced paper



- J.-S. Wang, and R. Mittra, "Finite Element Analysis of MMIC Structures and Electronic Packages Using Absorbing Boundary Conditions," IEEE. Trans. Microwave Theory and Techniques, vol. 42, no. 3, March 1994, pp. 441-449.

# Slotline Step

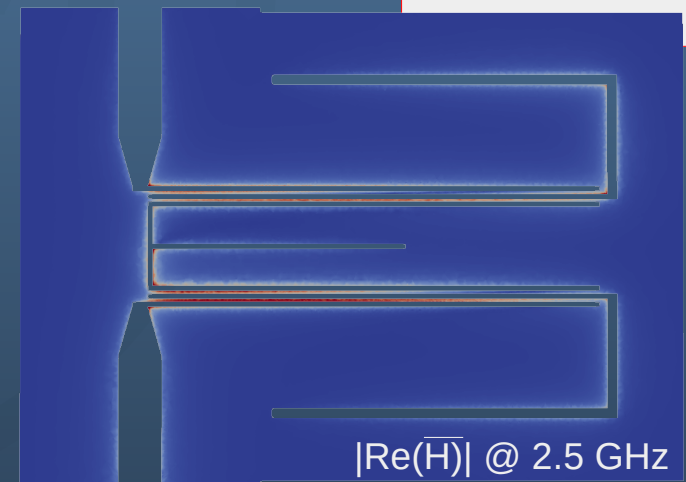
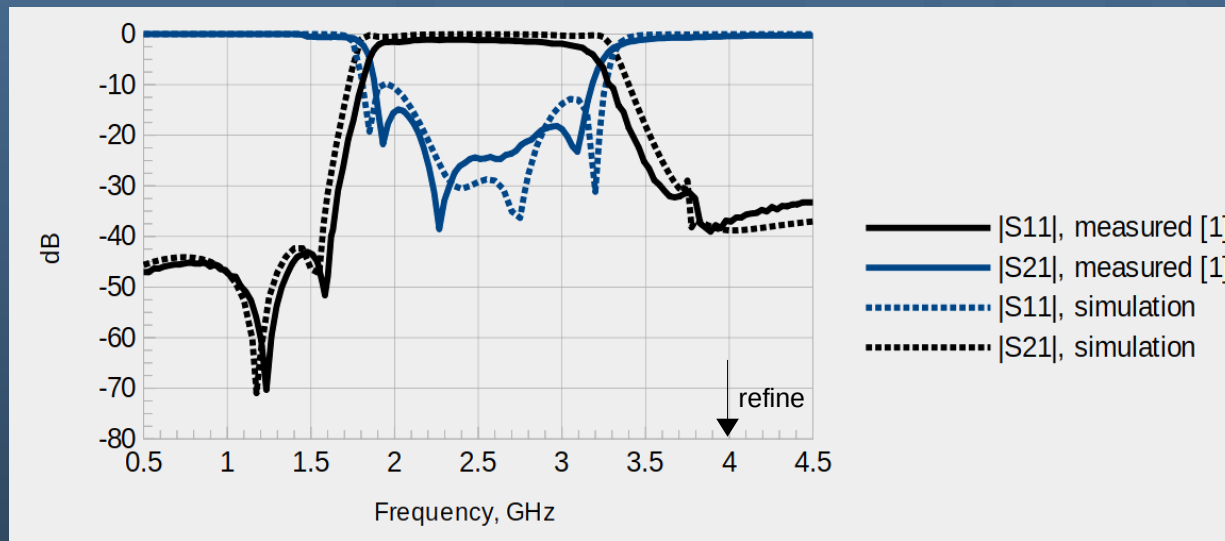
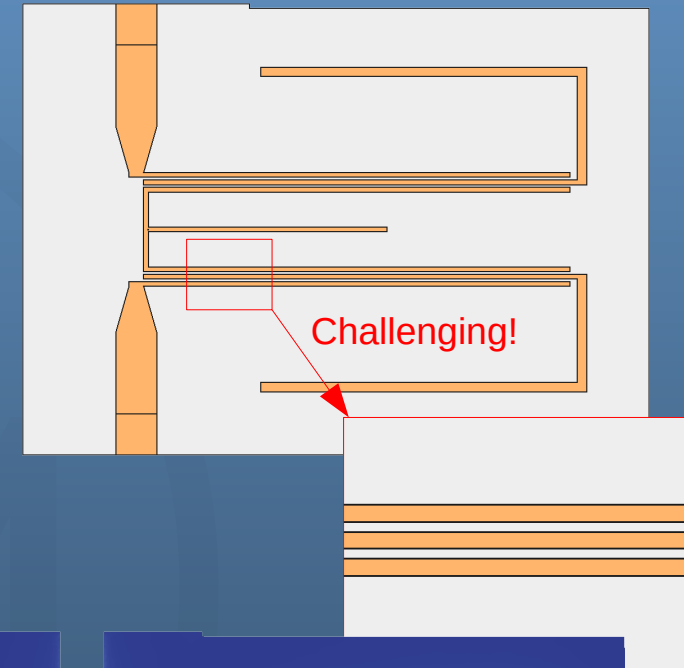
- $\frac{1}{2}$  slotline on symmetry
- substrate with  $\epsilon_r=2.22$
- 3rd order finite elements with 11 passes of AMR at 35 GHz with 0.001 convergence criteria
- Excellent agreement between this work and the referenced paper



- K. Hirayama, Md. Alam, Y. Hayashi, and M. Koshiba, "Vector Finite Element Method with Mixed-Interpolation-Type Triangular-Prism Element for Waveguide Discontinuities," IEEE Trans. Microwave Theory and Techniques, vol. 42, no. 12, Dec. 1994, pp. 2311-2316.

# Microstrip Filter

- Simulation with dielectric losses only
  - conductor losses not yet supported
- 2<sup>nd</sup> order elements
- AMR with 9 iterations at 4 GHz with 0.02 convergence criteria
- Good agreement considering the differences in losses



1 W.-C. Weng, "Design and Optimization of Compact Microstrip Wideband Bandpass Filter Using Taguchi's Method," *IEEE Open Access Journal*, vol. 10, 2022, pp. 107242-107249.



# Regression Suites

- Automated
- With and without AMR
- OpenParEM2D
  - 27 test cases
    - Microstrip, stripline, coax, rectangular waveguide, loaded rectangular waveguide
  - 43,738 checks
- OpenParEM3D
  - 17 test cases
    - Microstrip, slotline, rectangular waveguide, loaded rectangular waveguide
    - Orientation variations (i.e. rotations in space)
  - 390 checks

# Conclusions

- An effective 3D full-wave time-harmonic EM simulator for the calculation of S-parameters is outlined and demonstrated to produce high accuracy
- Lack of support for the gradient term  $\nabla_t E_n$  on boundaries has two consequences
  - non-TE modes at ports require de-embedding (should be rare)
  - 2X run-time increase to separate forward and backward waves at the driving port due to the need to calculate  $\bar{H}$
- To Do
  - Add impedance boundary condition for losses and antennas
  - Add PML for absorbing boundary condition at ports
  - Write documentation
  - Release

Thanks to LLNL's Mark Stowell for many very helpful email exchanges.